Explicit Maths Instruction in the Primary Classroom

MULTIPLICATION FACTS – x3	SQUARE NUMBERS - EXPONENTS	VERTICAL MULTIPLICATION ALGORITHM
$4 \times 3 = 12$ $6 \times 3 = 18$ $8 \times 3 = 24$ $7 \times 3 = 21$ $2 \times 3 = 6$ $10 \times 3 = 30$ $3 \times 3 = 9$ $9 \times 3 = 27$ $1 \times 3 = 3$ $5 \times 3 = 15$ $3 \times 30 = 90$ $300 \times 30 = 9000$	A square number is the product of a number multiplied by itself. Exponential notation is used to express square numbers. ² is the exponent. It tells us to multiply 16 by itself. $16^2 = 16 \times 16 = 256$	Write the following questions on your whiteboard vertically and solve. Make sure you say the algorithm softly to yourself while you work. $ \begin{array}{ccccccccccccccccccccccccccccccccccc$
$999 \times 3 = 2,997$ $97 \times 43 = 4,171$ $2,553 \times 3 = 7,659$	16 is the base.	$\frac{+2900}{3016} \qquad \frac{+5360}{5963} \qquad \frac{+51180}{+767700}_{822292}$

David Morkunas Classroom Teacher

@DaveMorkunas Bentleigh West Primary School

Session Outline

- About me
- Bentleigh West Primary School background and journey
- Low Variance Curriculum
- Timetable overview
- Standard algorithms for the four operations
- Problem solving and worded problems: CUBES and bar model
- A typical mathematics lesson in Grade 4
- Problem solving
- Daily reviews in Mathematics
- Q&A

About Me

- Worked as a financial auditor for PwC
- Chose to study teaching at 27
- Applied to ~70 schools, eventually landed at BWPS
- Particular passion for teaching maths and the role that memory plays in learning
- Huge nerd

Bentleigh West Primary School

- Previously considered a "coasting" school
- Began moving towards evidence-based instruction in late 2015
- Schools teach biologically secondary knowledge
- Explicit Direct Instruction (EDI)
 - Links well to Rosenshine's Principles of Instruction
 - Checking for Understanding, Obtaining a High Success Rate, Daily Review
 - Aligns to HITS (Multiple Exposures, Questioning)
- Definition of learning: change in long-term memory
 - Kirschner, Sweller, and Clark
 - Multiple exposures required to facilitate this

A Caveat...



Student Outcomes

2022 NAPLAN

Grade 3 Numeracy: 485

Grade 5 Numeracy: 556

66% of Grade 5 students achieved scores in the top 2 bands

4% of Grade 5 students scored in the bottom 2 bands

Low Variance Curriculum

- Developed at the end of the 2017 school year; rolled out first in 2018
- Allows teachers to focus on how to teach, not what to teach
- Minimises variance in instruction

Week	Number and Algebra	Number and Algebra	Statistics and Probability OR Measurement and Geometry	Worded Problems/Problem Solving
T1W1	Read (review) and order numbers to 5 digits (worksheet/presentation practice) Order 5-digit numbers in ascending and descending order	Greater than, less than Compare values using greater than and less than symbol.	LI: read analogue clocks to the nearest second	No Lesson
T1W2	LI: read and model 6 digits numbers and their place value	LI: order 6-digit numbers in ascending and descending order.	LI: convert between 12 and 24 hour time	Review Part/Part/Whole bar model (subtraction and addition). Use flow chart.
T1W3	LI: solve 5-digit addition problems with renaming using the vertical algorithm	LI: order 6-digit numbers on number lines	LI: select appropriate units to measure capacity	Review Part/Part/Whole bar model (multiplication and division). Use flow chart.
T1W4	L1: solve 5-digit subtraction problems with renaming using the vertical algorithm	LI: solve 2x2 digit multiplication using the area method.	LI: convert between units of measurement using place value (mass).	3/4 Maths Model Drawing 2.11 Example Ben has twice as many stickers as Jim. Ken has 65 more stickers than Ben. The three boys have 945 stickers altogether. How many stickers does Ken have? <u>https://youtu.be/iaCH4R1j7ew</u> SBM Unit A – Lesson 1
T1W5	LI: Solve 5-digit subtraction problems with internal zeroes	LI: solve 2x2-digit multiplication problems using the vertical algorithm Needs to be a 2x1-digit lesson next year	Select appropriate units of length Convert between units of measurement using place value (length).	3/4 Maths Model Drawing 2.12 Example Ben has twice as many stickers as Jim. Ken has 85 fewer stickers than Ben. The three boys have 945 stickers altogether. How many stickers does Ken have? <u>https://youtu.be/amga4VsGFUs</u> SBM Unit A – Lesson 2

Timetable

90 mins of Mathematics daily

Maths Review (30 mins)

- wide selection of previously-taught material
- used principles of spaced, interleaved, and retrieval practice
- PPT used from Monday to Thursday, independent maths quiz on Friday

New Waves Mental Maths (15 mins)

- From Monday to Wednesday this is teacher-modelled
- On Thursday and Friday, students complete independently

Maths Lesson (45 mins)

- New content (as per LVC)
- Monday and Wednesday: Number & Algebra
- Tuesday: Problem Solving (bar model)
- Thursday: Measurement & Geometry or Statistics & Probability
- Friday: Reteach

Timetable

Monday	Tuesday	Wednesday	Thursday	Friday
Maths Review PPT	Maths Review PPT	Maths Review PPT	Maths Review PPT	Independent Maths Quiz
30 mins	30 mins	30 mins	30 mins	30 mins
New Waves	New Waves	New Waves	New Waves	New Waves
Mental Maths	Mental Maths	Mental Maths	Mental Maths	Mental Maths
Teacher-led, 15 mins	Teacher-led, 15 mins	Teacher-led, 15 mins	Independent, 15 mins	Independent, 15 mins
New Lesson Number & Algebra 45 mins	New Lesson Problem Solving 45 mins	New Lesson Number & Algebra 45 mins	New Lesson M&G or S&P 45 mins	Reteach 45 mins

Standard algorithms for the four operations

- Booker text and Dr. Stephen Norton videos
- Provide a scaffold for students
- Place value language is heavily embedded
- Requires students to have experience with renaming
- Scalable; can still be used to solve complex problems

VERTICAL ADDITION WITH RENAMING

With renaming: Always start with the place furthest to the right.

"1 hendreddasiderhoued ceals contents hundreds. 6 ones add 6 ones equals 12 ones " 6 terfs add 6 ones equals 12 ones " 6 terfs add 4 contest equals 10 terfs and reds."

"Rename as 1 trans? end, ed. tens."

Write the terress in the ternes collumn.

Write the temperature description of temperature desc

Move to the transdreds.

The answer is 702.

VERTICAL SUBTRACTION ALGORITHM

With renaming:

Always start with the place furthest to the right.

"I have Z benes, reals // takked takey a very a Structure of the second seco

Subtract the temsdreds.

VERTICAL MULTIPLICATION ALGORITHM

2 by 2 digit:

We start with the bottom-right digit.

Step 3: Multiplied by 66 conessee publis 21/8tones. "& tenesmultiplied by 66 conessee publis 21/8tones"." "Rename as 2 tem & eater 4" tens."

Step 2: Multiply the tenes by the tens.

"Add 2 term d cpc cbd se bout en 14 hundreds."

Add the two numbers to get our final answer. Add our big fat zero. Our answer is 1548.

LONG DIVISION

Step 1 - Divide
"Can 9 tens be shared among 4?"
"Yes."
"How many would each share receive?"
2 tens. Put this 2 in your answer.

Step 2 - Multiply
"How many tens have been shared out?"
2 x 4 = 8

Step 3 - Subtract
"How many tens are left?"
9 - 8 = 1

Step 4 – Drag Down

23r1 3 13 -12



Repeat these four steps until you have arrived at your answer.

Problem Solving

- CUBES and Singapore Bar Model approach
- Framework to deconstruct questions
- Useful scaffold for those with reading difficulties
- Worked examples

CUBES

Circle the key numbers,

Underline the question,

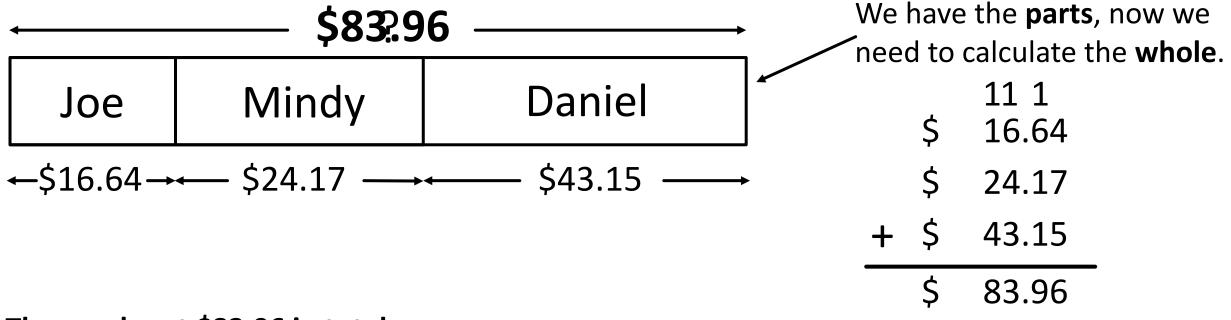
Box any maths action words,

Evaluate and draw,

Solve and check.

Adam had 3 ants. Bec had 5 ants. 3 + 5 = 8How many ants did they have in total? We use **CUBES** to solve worded problems.

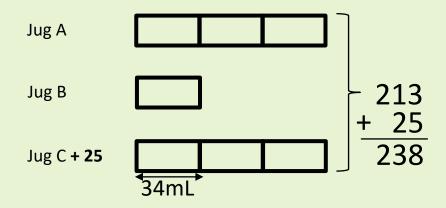
Joe's meal cost \$16.64. Mindy's meal cost \$24.17. Daniel's meal cost \$43.15. What was the total cost of the three meals? Circle the key numbers, Underline the question, Box any maths action words, Evaluate and draw, Solve and check.



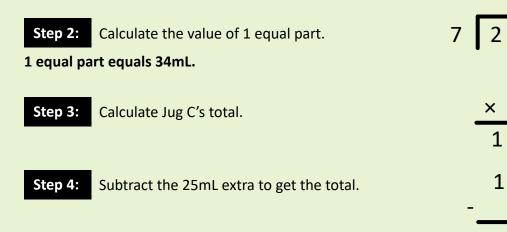
The meal cost \$83.96 in total.

Worked Example

Jug A contained three times as much olive oil as Jug B. Jug C contained 25mL less olive oil than Jug A. If the three jugs contained a total of 213mL of olive oil, how much did Jug C contain?



Step 1: Add the "fewer" onto the total. 7 equal parts equal 238mL.



Jug C contained 77mL of olive oil.

3 4	<u>L</u>
3 8	
3 4 3	
02	2
0 2 2 5	

77

Your Turn

Box A contained three times as much sugar as Box B. Box C contained 26g less sugar than Box A. If the three boxes contained a total of 184g of sugar, how much did Box C contain?

Box A	
Box B 184	
Box B Box C + 26 30g $184 + 26 - 210210$	
Step 1: Add the "fewer" onto the total.	
Step 2: Calculate the value of 1 equal part.	30 7210
Step 3: Calculate Box C's total.	30 × 3 90
Step 4: Subtract the 26g extra to get our answer.	90 - <u>26</u>
Box C contained 64g of sugar.	6 4

GRADE 4 – NUMBER & ALGEBRA

LEARNING INTENTION:

Use short division to solve problems with remainders

Use short division to solve problems with remainders ACTIVATE PRIOR KNOWLEDGE

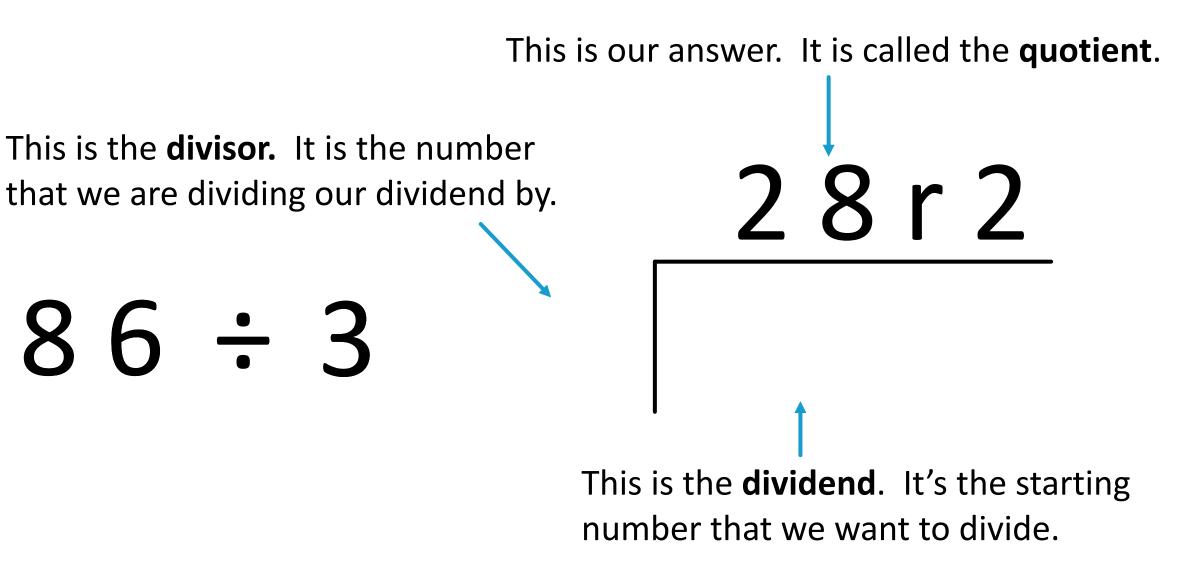
Solve these questions on your whiteboard.

П	
	/ 1
Н	• н

	1 5 r2	260r1	662r1
3	47	3 781 ⁶ -6 -	3973 36
•	3	 18	3 7
	17	-18	<u>- 36</u> 13
-	15	01 - 0	- 12
	2	1	1

You learned the **long division** algorithm a couple of weeks ago. Today we will cover the **short division** algorithm, which is a quicker way of solving these problems.

This is how we set up a division question.



I am trying to solve $89 \div 7$.

Is my question set up correctly? Finish these stems on your whiteboards.



89 7

This setup is immore the comment of the comments of the commen

This setup is immore the divident etce abute. fixed by swapping the dividend and the divisor.

This setup is immented in sorrected a. fix it before I begin solving.

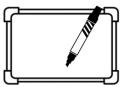
Here is how the question should look:

Short division is very similar to long division.

The main difference is that we do some of the steps in our heads.

Can we share 7 hundreds among 3? YES, DO IT! How many hundreds will each share receive? 2 How many hundreds remain? 1 Wenbegan with 77 tundseds and we've YES, DO IT! shared 6 of them (3 x 2), so there is 1 lefte? 5 How many tens remain? 2 Can we share 29 ones among 3? YES, DO IT! How many ones will each share receive? 9 How many ones remain? 2

Short division is very similar to long division. The main difference is that we do some of the steps **in our heads**.



47r3		
	Can we share 2 hundreds among 5?	NO, RENAME!
2 3 38	Can we share 23 tens among 5?	YES, DO IT!
	How many tens will each share receive?	4
	How many tens remain?	3
	Can we share 38 ones among 5?	YES, DO IT!
	How many ones will each share receive?	7
	How many ones remain?	3

Short division is very similar to long division.

2 2 8 4 r3

¹1³3¹9

The main difference is that we do some of the steps in our heads.

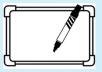


Can we share 9 thousands among 4?	YES, DO IT!
How many thousands will each share receive?	2
How many thousands remain?	1
Can we share 11 hundreds among 4?	YES, DO IT!
How many hundreds will each share receive?	2
How many hundreds remain?	3
Can we share 33 tens among 4?	YES, DO IT!
How many tens will each share receive?	8
How many tens remain?	1
Can we share 19 ones among 4?	YES, DO IT!
How many ones will each share receive?	4
How many ones remain?	3

Use short division to solve problems without remainders GUIDED PRACTICE

Solve the following questions on your whiteboard.

6



a)
$$33 \div 2$$

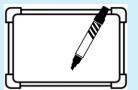
1 6 r1
2 $3^{1}3$
c) $6523 \div 7$
9 3 1 r
7 $6 5^{2}2^{1}3$

So why are we learning this?

- **Short division** is a much quicker algorithm to use when compared with **long division**. Getting comfortable with this will save a lot of time when solving division problems!

Use short division to solve problems without remainders SKILL CLOSURE

Solve the following questions on your whiteboard.



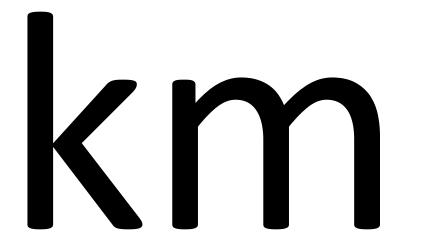
a) $57 \div 4$ 1 4 r1 4 $5^{1}7$ b) $871 \div 5$ 1 7 4 r1 5 $8^{3}7^{2}1$

a) 31÷2	b) 74÷5	<mark>c)</mark> 73÷3	<mark>d)</mark> 573÷4	<mark>e)</mark> 738÷5
1 5 r1 2 3 ¹ 1	1 4 r4 5 7 ² 4	2 4 r1 3 7 ¹ 3	1 4 3 r1 4 5 ¹ 7 ² 3	<u> </u>
<mark>f)</mark> 754÷3	<mark>g)</mark> 812÷	7 <mark>h)</mark> 9354	l÷8 i) 53	371÷6
251r1 37 ¹ 54	$\frac{116}{78^{1}1^{4}2}$	<u>1 1</u> 8 9 ¹ 3	<u>69r2</u> 5 ⁷ 4 6	<u>895r1</u> 53 ⁵ 7 ³ 1
<mark>j)*</mark> 37849÷12	<mark>k)*</mark> 75899 -	÷14 <mark>)*</mark> 819	9057 ÷ 23 m)	* 657984 ÷ 41
3 1 5 4 r 12 3 7 ¹ 8 ⁶ 4 ⁴ 9			$\frac{3 5 6 1 1 r4}{1^{12} 9^{14} 0^{2} 5^{2} 7} $ 41	1 6 0 4 8 r16 6 5 ²⁴ 7 ¹ 9 8 ³⁴ 4
n)* 917702÷6	54 <mark>o)*</mark> 849	9657 ÷ 75	<mark>p)*</mark> 999888777	÷ 137
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		1 3 3 2 8 r57 ⁹ 9 ²⁴ 9 ²⁴ 6 ²¹ 5 ⁶⁵ 7	7 2 9 8 137 9 9 9 ⁴⁰ 8 ¹³⁴ 8 ¹¹⁵ 8 ⁶	4 5 8 r31 ² 7 ⁷⁹ 7 ¹¹² 7

Daily Reviews

- Teaching a skill/concept once doesn't lead to mastery
- Regular review/multiple exposures help transfer knowledge to long-term memory
- Heavily supported by research
- Mini whiteboards
- Fast pace
- Great opportunity for formative assessment

UNITS OF MEASUREMENT



kilometres

2D SHAPES

scalene triangle

UNITS OF TIME

minutes in an hour



COMPASS DIRECTIONS

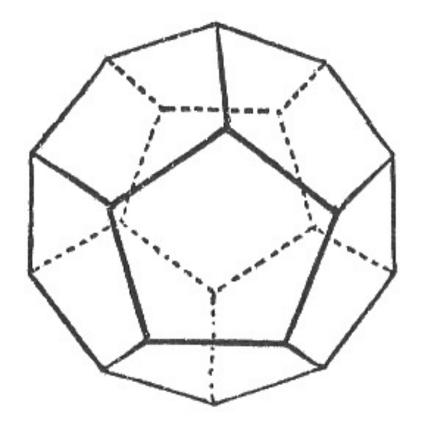


Northeast NE

MEASUREMENT CONVERSIONS

Sides on a pentagon?

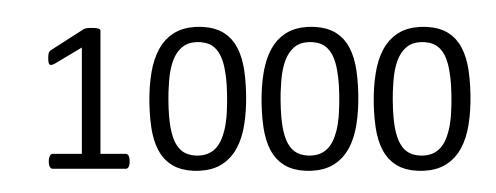
3D SOLIDS



dodecahedron

UNITS OF TIME

years in a millenium





Month after February? March

MULTIPLICATION FACTS – x8

 $1 \times 8 = 8$ $2 \times 8 = 16$ $3 \times 8 = 24$ $4 \times 8 = 32$ $5 \times 8 = 40$

 $6 \times 8 = 48$ $7 \times 8 = 56$ $8 \times 8 = 64$ $9 \times 8 = 72$ $10 \times 8 = 80$

MULTIPLICATION FACTS – x8



$1 \times 8 = 8$	3 x 8 = 24	6 x 8 = 48
10 x 8 = 80	7 x 8 = 56	8 x 8 = 64
2 x 8 = 16	5 x 8 = 40	9 x 8 = 72
4 x 8 = 32		
18 x 8 = 144	5 x 80 = 400	60 x 80 = 4,800
385 x 8 = 3,080	66 x 38 = 2,508	139 <mark>< 8 = 1,112</mark>

SKIP COUNTING BY 8s



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100



FACT FAMILIES

5 * 8 = 40

FACT FAMILIES

$7 \times 8 = 56$

VERTICAL ADDITION WITH RENAMING

Write the following questions on your whiteboard vertically and solve. Make sure you say the algorithm softly to yourself while you work.

<u>,</u> 11	11	. 21	1 11
a) 575	b) 4.63	c) 845	d) 8.637
+ 687	+ 3.89	667	+ 5.884
1262	8.52	+ 997	14.521
		2509	

SUBTRACTION ACROSS ZERO

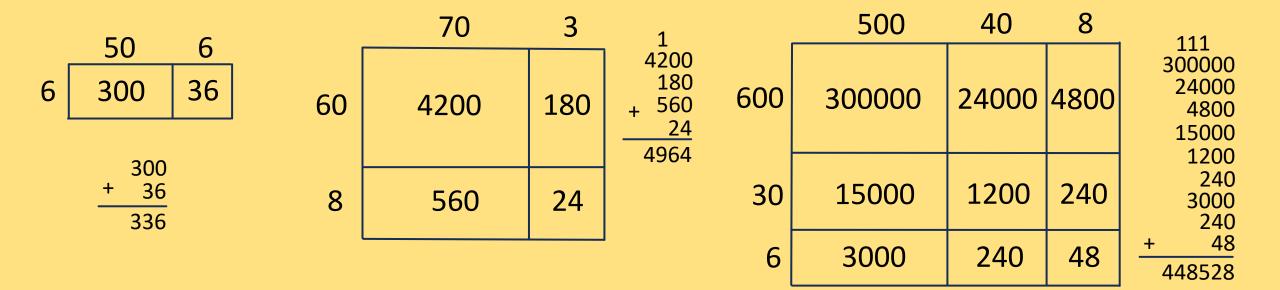
Write the following questions on your whiteboard vertically and solve. Make sure you say the algorithm softly to yourself while you work.

2911	4913	710	611 915
a) 30 1	b) 50 3	c) & Q.9	d) \72.0 5
- 167	- 327	<u> </u>	-45.68
134	176	25.2	26.37

MULTIPLICATION – AREA MODEL

Solve these questions using the area model.

a) 56 x 6 = 336 b) 73 x 68 = 4964 c) 548 x 636 = 448528





SHORT DIVISION

Solve the following problems using short division.

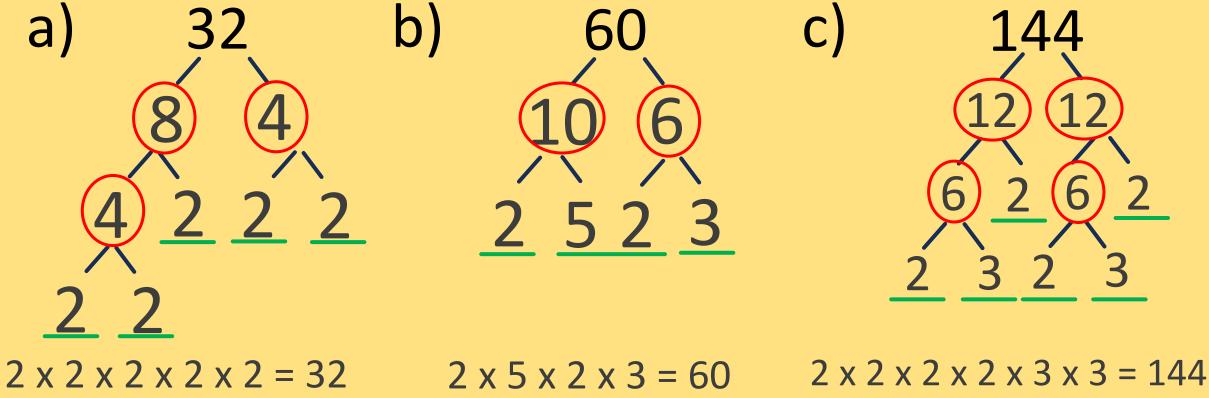
a) 4396 ÷ 3	b) 573÷6
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	95r3 657 ³ 3
c) 49624÷7	d) 758476÷37
7 0 8 9 r1	20499r13
7 4 9 6 2 ⁶ 4	37 7 5 ¹ 8 ¹⁸ 4 ³⁶ 7 ³⁴ 6

Convert the following mixed numbers into improper fractions.

a) $4\frac{1}{3} = \frac{13}{3}$ d) $7\frac{5}{9} = \frac{68}{9}$ e) $13\frac{7}{12} = \frac{163}{12}$ ^{b)} $6\frac{1}{2} = \frac{13}{2}$ c) $8\frac{2}{3} = \frac{26}{3}$ f) $243 \frac{13}{27} = \frac{6574}{27}$

PRIME FACTORISATION

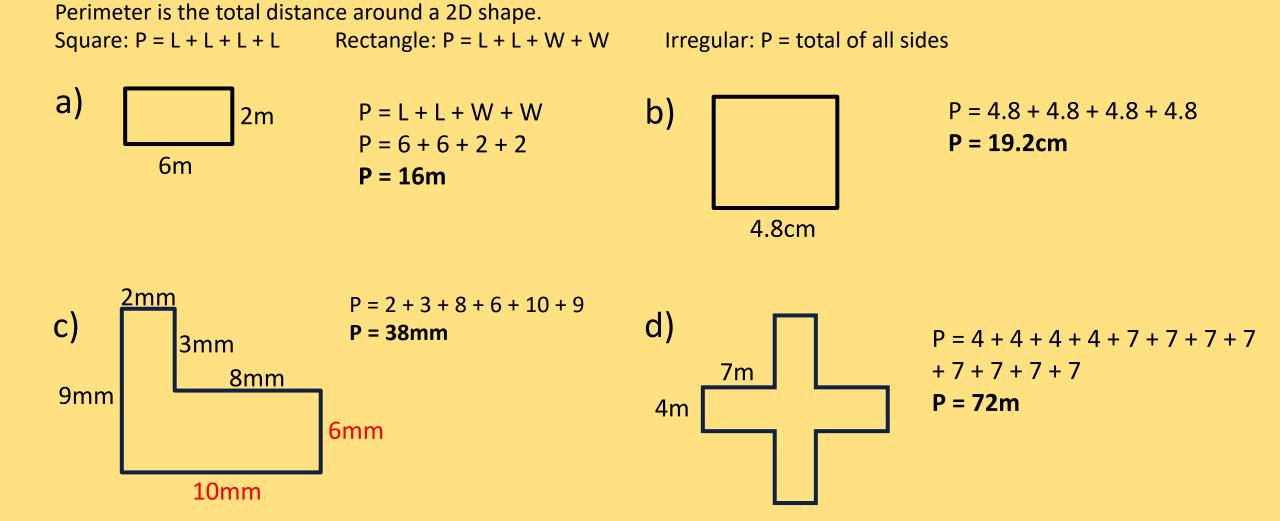
Create factor trees and determine the prime factors of the following numbers.



 $2^5 = 32$

 $2 \times 5 \times 2 \times 3 = 60$ $2^2 \times 3 \times 5 = 60$ $2 \times 2 \times 2 \times 2 \times 3 \times 3 = 144$ $2^4 \times 3^2 = 144$

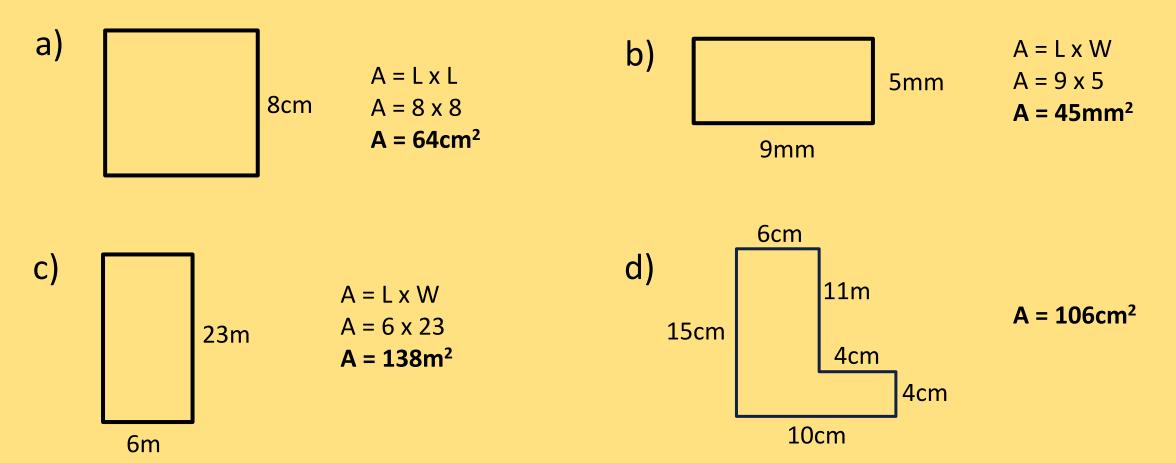
PERIMETER



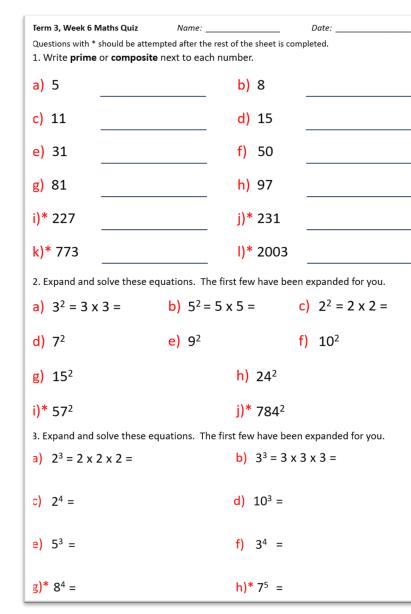
AREA

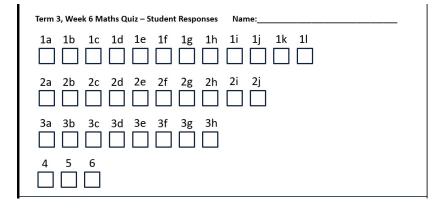


Area is the total space inside a 2D shape. Square: A = L x L Rectangle: A = L x W



Friday Maths Quiz





Friday Maths Quiz



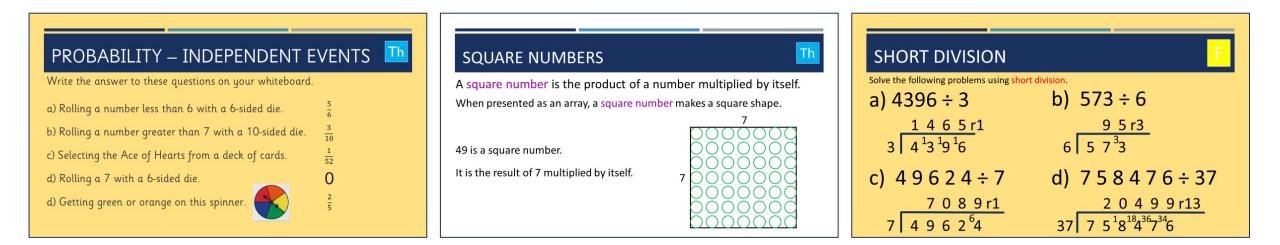
RESOURCES

- Booker, Bond, Sparrow & Swan Teaching Primary Mathematics

- Stephen Norton videos and PDF: Teaching And Learning Fundamental Mathematics

- Maths Model Drawing Made Easy and Inspiring

Q&A



Twitter: @DaveMorkunas